# Distributional similarity Introduction and implementation

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INCAS<sup>3</sup> WORKSHOP databases and annotating Wednesday 10 August, 2011

# Distributional similarity

- Most work on semantic similarity relies on the DISTRIBUTIONAL HYPOTHESIS (Harris 1954)
  - Take a word and its contexts:
    - tasty tnassiorc
    - greasy tnassiorc
    - *tnassiorc* with butter
    - *tnassiorc* for breakfast
- By looking at a word's context, one can infer its meaning

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  - Take a word and its contexts:  $\Rightarrow$  **FOOD** 
    - tasty tnassiorc
    - greasy tnassiorc
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Introduction Theory Implementation Similarity Context Weighting Dimensionality reduction

# Matrix

#### • Capture co-occurrence frequencies of two entities

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Similarity Context Weighting Dimensionality reduction



## • Capture co-occurrence frequencies of two entities

	rouge	délicieux	rapide	d'occasion
pomme	2	1	0	0
vin	2	2	0	0
voiture	1	0	1	2
camion	1	0	1	1

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## • Capture co-occurrence frequencies of two entities

	rouge	délicieux	rapide	d'occasion
pomme	7	9	0	0
vin	12	6	0	0
voiture	7	0	8	4
camion	2	0	3	4

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## • Capture co-occurrence frequencies of two entities

	rouge	délicieux	rapide	d'occasion
pomme	56	98	0	0
vin	44	34	0	0
voiture	23	0	31	39
camion	4	0	18	29

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## • Capture co-occurrence frequencies of two entities

	rouge	délicieux	rapide	d'occasion
pomme	728	592	1	0
vin	1035	437	0	2
voiture	392	0	487	370
camion	104	0	393	293

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# Similarity calculation

#### Cosine

• 
$$cos(\overrightarrow{x}, \overrightarrow{y}) = \frac{\overrightarrow{x} \cdot \overrightarrow{y}}{|\overrightarrow{x}||\overrightarrow{y}|} = \frac{\sum_{i=1}^{n} x_i y_i}{\sqrt{\sum_{i=1}^{n} x_i^2 \sum_{i=1}^{n} y_i^2}}$$

- Examples:
  - *cos*(*pomme*, *vin*) = .96
  - cos(pomme, voiture) = .42
- Other possibilities:
  - set-theoretic measures
    - Dice
    - Jaccard
  - probabilistic measures
    - Kullback-Leibler divergence
    - Jensen-Shannon divergence

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# Different kinds of context

- Three different word space models based on context:
  - document-based model (nouns  $\times$  documents)
  - window-based model (nouns × context words)
  - syntax-based model (nouns  $\times$  dependency relations)
- Each model with plethora of parameters!
  - document size, window size, type of dependency relations
  - weighting function
  - $\bullet~\pm$  dimensionality reduction

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# Document-based model

- Plain word corpus
- Matrix contains the number of times a word appears in a particular document (web page, newspaper article, wikipedia entry, ...)
- Parameters:
  - document size: full document, paragraph, ...
  - weighting: TF/IDF, logarithmic, ...

	doc1	doc2	doc3	doc4
word1				
word2				
word3				
word4				

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# Window-based model

- Plain word corpus
- Matrix contains the number of times a word appears in a particular window around a (small window, sentence, paragraph, ...)
- Parameters:
  - dependency relations: which ones?
  - weighting: TF/IDF, pointwise mutual information, logarithmic, ...

	word1	word2	word3	word4
word1				
word2				
word3				
word4				

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# Syntax-based model

- Syntactically annotated (automatically parsed) corpus
- Matrix contains the number of times a word appears with a particular syntactic (dependency) feature (apple: direct object of *eat*, bomb: subject of *explode*, ...)
- Parameters:
  - window size: n words (left/right), sentence, paragraph ...
  - weighting: TF/IDF, pointwise mutual information, logarithmic, ...

	dep1	dep2	dep3	dep4
word1				
word2				
word3				
word4				

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# Different kinds of semantic similarity

- 'tight', synonym-like similarity: (near-)synonymous or (co-)hyponymous
- **loosely related, topical similarity**: more loose relationships, such as association and meronymy

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# Different kinds of semantic similarity

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## Example

- médecin 'doctor': docteur 'doctor', médecin de famille 'family doctor', chirurgien 'surgeon', spécialiste 'specialist', dermatologue 'dermatologist', gynécologue 'gynaecologist'
- médecin 'doctor': malade 'patient', maladie 'disease', diagnostic 'diagnosis, traitement 'treatment, hôpital 'hospital', stéthoscope 'stethoscope'

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# Relation context – similarity

- Different context leads to different kind of similarity
- Syntax, small window  $\leftrightarrow$  large window, documents
- The former models induce tight, synonymous similarity
- The latter models induce topical relatedness

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# Relation context – similarity

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#### Evaluation

- Syntax-based model scores best when evaluated according to Wordnet similarity measures (CORNETTO)
- Large window and document-based do not score well on Wordnet similarity, but do score on Wordnet domain evaluation

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# Weighting

- How salient is a word within a document/window/dependency relation?
- de voetballer is  $\leftrightarrow$  de voetballer scoort
- Local vs. global weighting:
  - local: only based on information in matrix cell (e.g. logarithmic weighting)
  - global: based on global instances/feature frequencies (probabilities)

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local weighting: logarithmic weighting

• 
$$f_{i,j} = 1 + log(f_{i,j})$$

• smooths high frequency data

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# global weighting: pointwise mutual information

• 
$$pmi(i,j) = log(\frac{p(i,j)}{p(i)p(j)})$$

- Compare joint probability p(i, j) with marginal probabilities p(i) and p(j)
- higher value if *i* and *j* occur together more often than one would expect given their independence

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# **Dimensionality** reduction

- reduce large number of features to limited number of 'semantic dimensions'
- useful for topical similarity (dimensions represent topics)
- latent semantic analysis, latent dirichlet allocation, non-negative matrix factorization

Preprocessing Determination of instances and features Matrix construction Similarity computations

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# Python framework

## Preprocessing

- ② Determination of instances and features
- Matrix construction
- ④ Similarity computations

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# Preprocessing

- Convert corpus to proper format/usable form
  - convert to raw text
  - syntactic parsing
  - extraction of dependency triples
  - storage: plain text or MySQL database

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Image: A math a math

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# Read in corpus

- Parent Corpusreader class
- Child classes for specific corpus formats

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# Determination of instances and features

- instances (words) and features (window-based words, dependency features) need to be determined beforehand for proper matrix construction
  - 'dry run' on corpus
  - or initial sort for most frequent instances/features
  - or complete construction with pruning step

Preprocessing Determination of instances and features **Matrix construction** Similarity computations

## Matrix construction

- Matrices tend to be very sparse (dependency-based: <1% zeros)
- sparse matrix implementation: lists-of-hashes (lists-of-dicts)
- word strings mapped to integers (with translation dict)
- alternative: scientific libraries (Numpy/Scipy)

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# Matrix construction

- Parent Matrix class with
  - initial determination
  - fill options
  - weighting functions
  - normalization
- Child classes for specific models (document-based, window-based, dependency-based)

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# Similarity computations

- different similarity functions operating on vectors of matrix (cosine, KL-divergence, ...)
- functions of Matrix itself
- Numpy/Scipy